

EXPANDING AND CONDENSING LOGARITHMS

EXPANDING AND CONDENSING LOGARITHMS ARE FUNDAMENTAL CONCEPTS IN ALGEBRA AND LOGARITHMIC FUNCTIONS, PLAYING A CRUCIAL ROLE IN SIMPLIFYING COMPLEX LOGARITHMIC EXPRESSIONS AND SOLVING EQUATIONS EFFICIENTLY. MASTERING THESE TECHNIQUES ENABLES STUDENTS AND PROFESSIONALS ALIKE TO MANIPULATE LOGARITHMIC EXPRESSIONS WITH CONFIDENCE, WHETHER IN PURE MATHEMATICS, ENGINEERING, OR APPLIED SCIENCES. THIS ARTICLE PROVIDES AN IN-DEPTH EXPLORATION OF EXPANDING AND CONDENSING LOGARITHMS, ILLUSTRATING THEIR PROPERTIES, METHODS, AND PRACTICAL APPLICATIONS TO ENHANCE YOUR UNDERSTANDING AND PROBLEM-SOLVING SKILLS.

UNDERSTANDING LOGARITHMS: A BRIEF OVERVIEW

BEFORE DIVING INTO THE TECHNIQUES OF EXPANDING AND CONDENSING LOGARITHMS, IT'S ESSENTIAL TO GRASP WHAT LOGARITHMS ARE AND THEIR BASIC PROPERTIES.

WHAT IS A LOGARITHM?

A LOGARITHM IS THE INVERSE OPERATION OF EXPONENTIATION. FOR A POSITIVE REAL NUMBER $(a \neq 1)$, THE LOGARITHM BASE (a) OF A NUMBER (x) IS THE EXPONENT TO WHICH (a) MUST BE RAISED TO OBTAIN (x) :

$$\begin{aligned} & \text{If } \log_a x = y \text{ then } a^y = x \\ & \text{Conversely, if } a^y = x \text{ then } \log_a x = y \end{aligned}$$

COMMON LOGARITHM PROPERTIES

KEY PROPERTIES THAT FORM THE FOUNDATION FOR EXPANDING AND CONDENSING LOGARITHMS INCLUDE:

- PRODUCT PROPERTY: $\log_a(xy) = \log_a x + \log_a y$
- QUOTIENT PROPERTY: $\log_a\left(\frac{x}{y}\right) = \log_a x - \log_a y$
- POWER PROPERTY: $\log_a(x^k) = k \log_a x$

THESE PROPERTIES ARE INSTRUMENTAL FOR MANIPULATING LOGARITHMIC EXPRESSIONS IN VARIOUS FORMS.

EXPANDING LOGARITHMS

EXPANDING LOGARITHMS INVOLVES EXPRESSING A COMPLEX LOGARITHMIC EXPRESSION AS A SUM OR DIFFERENCE OF SIMPLER LOGARITHMS. THIS PROCESS IS PARTICULARLY USEFUL FOR SIMPLIFYING CALCULATIONS AND SOLVING EQUATIONS INVOLVING MULTIPLE LOGARITHMIC TERMS.

TECHNIQUES FOR EXPANDING LOGARITHMS

1. APPLYING THE PRODUCT PROPERTY

WHEN YOU ENCOUNTER A LOGARITHM OF A PRODUCT, EXPAND IT INTO THE SUM OF THE LOGARITHMS:

$$\log_a(xy) = \log_a x + \log_a y$$

EXAMPLE:

$$\backslash[\backslash\text{LOG}_2(8 \times 4) = \backslash\text{LOG}_2 8 + \backslash\text{LOG}_2 4 = 3 + 2 = 5\backslash]$$

2. APPLYING THE QUOTIENT PROPERTY

FOR A LOGARITHM OF A QUOTIENT, EXPAND IT INTO THE DIFFERENCE OF LOGARITHMS:

$$\backslash[\backslash\text{LOG}_A \left(\frac{X}{Y}\right) = \backslash\text{LOG}_A X - \backslash\text{LOG}_A Y\backslash]$$

EXAMPLE:

$$\backslash[\backslash\text{LOG}_3 \frac{27}{9} = \backslash\text{LOG}_3 27 - \backslash\text{LOG}_3 9 = 3 - 2 = 1\backslash]$$

3. APPLYING THE POWER PROPERTY

WHEN THE ARGUMENT OF A LOGARITHM IS RAISED TO A POWER, EXPAND IT BY BRINGING THE EXPONENT IN FRONT:

$$\backslash[\backslash\text{LOG}_A X^k = k \backslash\text{LOG}_A X\backslash]$$

EXAMPLE:

$$\backslash[\backslash\text{LOG}_5 125^2 = 2 \backslash\text{LOG}_5 125 = 2 \times 3 = 6\backslash]$$

4. EXPANDING NESTED LOGARITHMS

IN EXPRESSIONS WHERE MULTIPLE PROPERTIES APPLY, COMBINE THE STEPS:

EXAMPLE:

EXPAND $\backslash(\backslash\text{LOG}_2(8x^3))\backslash$:

$$\backslash[\backslash\text{LOG}_2 8 + \backslash\text{LOG}_2 x^3 = 3 + 3 \backslash\text{LOG}_2 x\backslash]$$

PRACTICAL APPLICATIONS OF EXPANDING LOGARITHMS

- SIMPLIFYING COMPLEX LOGARITHMIC EXPRESSIONS FOR EASIER COMPUTATION.
- CONVERTING PRODUCTS, QUOTIENTS, AND POWERS INTO ADDITIVE OR SUBTRACTIVE FORMS.
- FACILITATING THE SOLVING OF LOGARITHMIC EQUATIONS.

CONDENSING LOGARITHMS

CONDENSING LOGARITHMS IS THE REVERSE PROCESS OF EXPANDING. IT INVOLVES REWRITING A SUM OR DIFFERENCE OF

LOGARITHMS AS A SINGLE LOGARITHMIC EXPRESSION WITH A COMBINED ARGUMENT. THIS TECHNIQUE SIMPLIFIES COMPLEX EXPRESSIONS AND IS VALUABLE FOR SOLVING EQUATIONS MORE STRAIGHTFORWARDLY.

TECHNIQUES FOR CONDENSING LOGARITHMS

1. USING THE PRODUCT PROPERTY

COMBINE MULTIPLE LOGARITHMS WITH ADDITION INTO A SINGLE LOGARITHM WITH A PRODUCT ARGUMENT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A } X + \backslash\text{LOG_A } Y = \backslash\text{LOG_A } (XY) \\ & \backslash] \end{aligned}$$

EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_2 } 3 + \backslash\text{LOG_2 } 4 = \backslash\text{LOG_2 } (3 \times 4) = \backslash\text{LOG_2 } 12 \\ & \backslash] \end{aligned}$$

2. USING THE QUOTIENT PROPERTY

COMBINE LOGARITHMS WITH SUBTRACTION INTO A SINGLE LOGARITHM WITH A QUOTIENT ARGUMENT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A } X - \backslash\text{LOG_A } Y = \backslash\text{LOG_A } \left(\frac{X}{Y}\right) \\ & \backslash] \end{aligned}$$

EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_5 } 20 - \backslash\text{LOG_5 } 4 = \backslash\text{LOG_5 } \left(\frac{20}{4}\right) = \backslash\text{LOG_5 } 5 = 1 \\ & \backslash] \end{aligned}$$

3. USING THE POWER PROPERTY

EXPRESS A MULTIPLE OF A LOGARITHM AS A SINGLE LOGARITHM WITH A POWER:

$$\begin{aligned} & \backslash[\\ & k \backslash\text{LOG_A } X = \backslash\text{LOG_A } X^k \\ & \backslash] \end{aligned}$$

EXAMPLE:

$$\begin{aligned} & \backslash[\\ & 3 \backslash\text{LOG_2 } 7 = \backslash\text{LOG_2 } 7^3 = \backslash\text{LOG_2 } 343 \\ & \backslash] \end{aligned}$$

4. CONDENSING EXPRESSIONS WITH MULTIPLE TERMS

WHEN DEALING WITH MULTIPLE TERMS:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A } X + \backslash\text{LOG_A } Y - \backslash\text{LOG_A } Z = \backslash\text{LOG_A } \frac{XY}{Z} \\ & \backslash] \end{aligned}$$

EXAMPLE:

$$\log_2 3 + \log_2 8 - \log_2 4 = \log_2 \frac{3 \times 8}{4} = \log_2 6$$

APPLICATIONS OF CONDENSING LOGARITHMS

- SIMPLIFYING COMPLEX LOGARITHMIC EXPRESSIONS FOR EASIER EVALUATION.
- TRANSFORMING MULTIPLE LOGS INTO A SINGLE LOG TO FACILITATE SOLVING LOGARITHMIC EQUATIONS.
- MAKING INEQUALITIES INVOLVING LOGARITHMS MORE MANAGEABLE.

PRACTICAL EXAMPLES AND PROBLEM-SOLVING STRATEGIES

TO SOLIDIFY YOUR UNDERSTANDING, CONSIDER THE FOLLOWING PROBLEM-SOLVING APPROACHES USING EXPANDING AND CONDENSING TECHNIQUES.

EXAMPLE 1: EXPANDING A COMPLEX LOGARITHM

PROBLEM:

SIMPLIFY $\log_3 (81x^2y)$.

SOLUTION:

STEP 1: RECOGNIZE THE COMPONENTS:

$$\log_3 81 + \log_3 x^2 + \log_3 y$$

STEP 2: SIMPLIFY KNOWN LOGS:

$$\log_3 81 = 4 \quad \text{SINCE} \quad 3^4 = 81$$

STEP 3: APPLY THE POWER PROPERTY:

$$4 + 2 \log_3 x + \log_3 y$$

FINAL EXPRESSION:

$$4 + 2 \log_3 x + \log_3 y$$

EXAMPLE 2: CONDENSING A LOGARITHMIC EXPRESSION

PROBLEM:

Express $(\log_2 5 + 3 \log_2 2 - \log_2 7)$ as a single logarithm.

Solution:

Step 1: Use the power property:

$$\log_2 5 + \log_2 2^3 - \log_2 7$$

which simplifies to:

$$\log_2 5 + \log_2 8 - \log_2 7$$

Step 2: Combine the first two:

$$\log_2 (5 \times 8) - \log_2 7 = \log_2 40 - \log_2 7$$

Step 3: Use the quotient property:

$$\log_2 \left(\frac{40}{7} \right)$$

Final Expression:

$$\boxed{\log_2 \left(\frac{40}{7} \right)}$$

Common Mistakes and Tips for Mastery

- Remember the properties: Always verify which property applies before expanding or condensing.
- Watch for nested logs: Carefully handle multiple properties in complex expressions.
- Simplify step-by-step: Break down expressions into manageable parts.
- Check the domain: Logarithms are defined for positive arguments; ensure your transformations preserve this.

Conclusion

Expanding and condensing logarithms are essential skills that streamline the process of manipulating and solving logarithmic expressions. By understanding and applying the core properties—product, quotient, and power—one can transform complex logarithmic formulas into more manageable forms. Whether simplifying expressions for calculation, solving equations, or proving identities, mastering these techniques enhances mathematical fluency and problem-solving efficiency.

Regular practice with diverse problems will deepen your comprehension and enable you to recognize the most effective approach in any logarithmic scenario. Keep exploring the properties, and you'll find that expanding and condensing logarithms become intuitive tools in your mathematical toolkit.

FREQUENTLY ASKED QUESTIONS

WHAT IS THE BASIC PROPERTY OF EXPANDING LOGARITHMS?

THE BASIC PROPERTY OF EXPANDING LOGARITHMS IS THAT $\log(A \cdot B) = \log(A) + \log(B)$, WHICH ALLOWS US TO SPLIT A LOGARITHM OF A PRODUCT INTO THE SUM OF TWO LOGARITHMS.

HOW DO YOU EXPAND A LOGARITHM OF A POWER, SUCH AS $\log(A^n)$?

TO EXPAND A LOGARITHM OF A POWER, USE THE PROPERTY $\log(A^n) = n \log(A)$, WHICH ALLOWS YOU TO BRING THE EXPONENT IN FRONT OF THE LOGARITHM.

WHAT IS THE PROCESS OF CONDENSING LOGARITHMS?

CONDENSING LOGARITHMS INVOLVES COMBINING MULTIPLE LOGS INTO A SINGLE LOGARITHM USING PROPERTIES LIKE $\log(A) + \log(B) = \log(A \cdot B)$ AND $n \log(A) = \log(A^n)$.

HOW CAN YOU CONDENSE A SUM OF LOGARITHMS INTO A SINGLE LOGARITHM?

YOU CAN CONDENSE A SUM OF LOGARITHMS BY REWRITING IT AS A SINGLE LOGARITHM: $\log(A) + \log(B) = \log(A \cdot B)$. SIMILARLY, MULTIPLE TERMS CAN BE COMBINED BY MULTIPLYING THEIR ARGUMENTS.

WHAT IS THE SIGNIFICANCE OF EXPANDING AND CONDENSING LOGARITHMS IN SOLVING EQUATIONS?

EXPANDING AND CONDENSING LOGARITHMS SIMPLIFY COMPLEX LOGARITHMIC EXPRESSIONS, MAKING IT EASIER TO SOLVE EQUATIONS INVOLVING LOGARITHMS BY TRANSFORMING THEM INTO MORE MANAGEABLE FORMS.

ARE THE PROPERTIES OF EXPANDING AND CONDENSING LOGARITHMS APPLICABLE TO ALL TYPES OF LOGARITHMS?

YES, THESE PROPERTIES ARE APPLICABLE TO ALL LOGARITHMS WITH THE SAME BASE, SUCH AS COMMON LOGARITHMS (BASE 10) OR NATURAL LOGARITHMS (BASE e), AS LONG AS THE BASE REMAINS CONSISTENT.

CAN EXPANDING AND CONDENSING LOGARITHMS HELP IN CALCULUS PROBLEMS?

ABSOLUTELY, EXPANDING AND CONDENSING LOGARITHMS ARE USEFUL IN CALCULUS FOR SIMPLIFYING DERIVATIVES AND INTEGRALS INVOLVING LOGARITHMIC FUNCTIONS, AIDING IN MORE STRAIGHTFORWARD CALCULATIONS.

ADDITIONAL RESOURCES

EXPANDING AND CONDENSING LOGARITHMS: A COMPREHENSIVE GUIDE

LOGARITHMS ARE FUNDAMENTAL TOOLS IN MATHEMATICS, ESPECIALLY IN FIELDS LIKE ALGEBRA, CALCULUS, COMPUTER SCIENCE, AND ENGINEERING. THEY SERVE AS THE INVERSE OF EXPONENTIAL FUNCTIONS AND ARE ESSENTIAL FOR SOLVING EQUATIONS INVOLVING EXPONENTIAL GROWTH OR DECAY, AS WELL AS FOR SIMPLIFYING COMPLEX EXPRESSIONS. AMONG THE VARIOUS TECHNIQUES INVOLVING LOGARITHMS, EXPANDING AND CONDENSING LOGARITHMIC EXPRESSIONS ARE PARTICULARLY USEFUL FOR SIMPLIFYING CALCULATIONS, SOLVING EQUATIONS, AND UNDERSTANDING THE PROPERTIES OF LOGARITHMS MORE DEEPLY. THIS GUIDE EXPLORES THESE TECHNIQUES IN DETAIL, PROVIDING INSIGHTS, FORMULAS, AND PRACTICAL APPLICATIONS.

UNDERSTANDING LOGARITHMS: A BRIEF OVERVIEW

BEFORE DIVING INTO EXPANSION AND CONDENSATION, IT IS CRUCIAL TO UNDERSTAND WHAT LOGARITHMS ARE AND THEIR FUNDAMENTAL PROPERTIES.

DEFINITION OF A LOGARITHM

- THE LOGARITHM OF A NUMBER (x) WITH BASE (a) IS THE EXPONENT TO WHICH (a) MUST BE RAISED TO PRODUCE (x) :

$$\left[\begin{array}{l} \log_a x = y \quad \text{IF AND ONLY IF} \quad a^y = x \end{array} \right]$$

- NOTATION: $(\log_a x)$

KEY PROPERTIES OF LOGARITHMS

- PRODUCT RULE:

$$\left[\log_a (xy) = \log_a x + \log_a y \right]$$

- QUOTIENT RULE:

$$\left[\log_a \left(\frac{x}{y} \right) = \log_a x - \log_a y \right]$$

- POWER RULE:

$$\left[\log_a (x^k) = k \log_a x \right]$$

- CHANGE OF BASE FORMULA:

$$\left[\log_a x = \frac{\log_b x}{\log_b a} \right]$$

THESE PROPERTIES FORM THE FOUNDATION FOR EXPANDING AND CONDENSING LOGARITHMIC EXPRESSIONS.

EXPANDING LOGARITHMS: BREAKING DOWN COMPLEX EXPRESSIONS

EXPANDING LOGARITHMS INVOLVES EXPRESSING A SINGLE LOGARITHM OF A COMPLEX EXPRESSION AS A SUM OR DIFFERENCE OF SIMPLER LOGARITHMS. THIS PROCESS RELIES HEAVILY ON THE PRODUCT, QUOTIENT, AND POWER RULES OUTLINED ABOVE.

PURPOSE OF EXPANDING LOGARITHMS

- SIMPLIFY COMPLEX LOGARITHMIC EXPRESSIONS TO FACILITATE CALCULATIONS
- MAKE IT EASIER TO COMBINE OR COMPARE DIFFERENT LOGARITHMIC TERMS
- PREPARE EXPRESSIONS FOR SOLVING EQUATIONS
- AID IN DIFFERENTIATION AND INTEGRATION INVOLVING LOGARITHMS

TECHNIQUES FOR EXPANDING LOGARITHMIC EXPRESSIONS

1. APPLYING THE PRODUCT RULE:

- WHEN THE ARGUMENT OF THE LOGARITHM IS A PRODUCT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A}(XY) = \backslash\text{LOG_A} X + \backslash\text{LOG_A} Y \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_2}(8 \times 4) = \backslash\text{LOG_2} 8 + \backslash\text{LOG_2} 4 = 3 + 2 = 5 \\ & \backslash] \end{aligned}$$

2. APPLYING THE QUOTIENT RULE:

- WHEN THE ARGUMENT IS A QUOTIENT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A} \left(\frac{X}{Y} \right) = \backslash\text{LOG_A} X - \backslash\text{LOG_A} Y \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_3} \frac{81}{9} = \backslash\text{LOG_3} 81 - \backslash\text{LOG_3} 9 = 4 - 2 = 2 \\ & \backslash] \end{aligned}$$

3. APPLYING THE POWER RULE:

- WHEN THE ARGUMENT IS AN EXPONENTIAL:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_A} X^k = k \backslash\text{LOG_A} X \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG_5}(125^2) = 2 \backslash\text{LOG_5} 125 = 2 \times 3 = 6 \\ & \backslash] \end{aligned}$$

SINCE $\backslash(125 = 5^3 \backslash)$.

4. HANDLING NESTED OR MULTIPLE OPERATIONS:

- BREAK DOWN STEP-BY-STEP, PRIORITIZING THE APPLICATION OF THE RULES TO SIMPLIFY THE EXPRESSION INTO A SUM OR DIFFERENCE OF SINGLE LOGARITHMS.

CONDENSING LOGARITHMS: COMBINING MULTIPLE LOGARITHMS INTO A SINGLE EXPRESSION

CONDENSING IS THE INVERSE PROCESS OF EXPANDING. IT INVOLVES COMBINING MULTIPLE LOGARITHMIC TERMS INTO A SINGLE LOGARITHM, OFTEN TO SIMPLIFY EXPRESSIONS OR TO PREPARE FOR SOLVING EQUATIONS.

PURPOSE OF CONDENSING LOGARITHMS

- SIMPLIFY THE EXPRESSION TO A MORE MANAGEABLE FORM
- FACILITATE SOLVING LOGARITHMIC EQUATIONS
- RECOGNIZE AND UTILIZE THE PROPERTIES OF LOGARITHMS MORE EASILY
- MAKE EXPRESSIONS MORE SUITABLE FOR SUBSTITUTION OR FURTHER ALGEBRAIC MANIPULATION

TECHNIQUES FOR CONDENSING LOGARITHMIC EXPRESSIONS

1. USING THE PRODUCT RULE FOR CONDENSATION:

- CONVERT A SUM OF LOGARITHMS INTO A SINGLE LOGARITHM WITH A PRODUCT ARGUMENT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG}_A X + \backslash\text{LOG}_A Y = \backslash\text{LOG}_A (XY) \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG}_2 3 + \backslash\text{LOG}_2 4 = \backslash\text{LOG}_2 (3 \times 4) = \backslash\text{LOG}_2 12 \\ & \backslash] \end{aligned}$$

2. USING THE QUOTIENT RULE FOR CONDENSATION:

- CONVERT A DIFFERENCE OF LOGARITHMS INTO A SINGLE LOGARITHM WITH A QUOTIENT ARGUMENT:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG}_A X - \backslash\text{LOG}_A Y = \backslash\text{LOG}_A \left(\frac{X}{Y}\right) \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & \backslash\text{LOG}_5 20 - \backslash\text{LOG}_5 4 = \backslash\text{LOG}_5 \left(\frac{20}{4}\right) = \backslash\text{LOG}_5 5 = 1 \\ & \backslash] \end{aligned}$$

3. USING THE POWER RULE FOR CONDENSATION:

- WHEN MULTIPLYING A LOGARITHM BY A COEFFICIENT, EXPRESS IT AS A POWER INSIDE A SINGLE LOGARITHM:

$$\begin{aligned} & \backslash[\\ & k \backslash\text{LOG}_A X = \backslash\text{LOG}_A X^k \\ & \backslash] \end{aligned}$$

- EXAMPLE:

$$\begin{aligned} & \backslash[\\ & 3 \backslash\text{LOG}_2 7 = \backslash\text{LOG}_2 7^3 = \backslash\text{LOG}_2 343 \\ & \backslash] \end{aligned}$$

4. COMBINING MULTIPLE LOGARITHMS:

- FOR EXPRESSIONS WITH MULTIPLE TERMS, APPLY THE RULES SEQUENTIALLY:

$$\left[\log_a x + \log_a y - \log_a z = \log_a \left(\frac{xy}{z} \right) \right]$$

- EXAMPLE:

$$\left[2 \log_3 2 + \log_3 8 - \log_3 4 = \log_3 2^2 + \log_3 8 - \log_3 4 \right]$$

$$\left[= \log_3 4 + \log_3 8 - \log_3 4 = \log_3 4 + \log_3 8 - \log_3 4 \right]$$

$$\left[= \log_3 8 \right]$$

- OR, MORE GENERALLY:

$$\left[\log_a x + \log_a y - \log_a z = \log_a \left(\frac{xy}{z} \right) \right]$$

PRACTICAL APPLICATIONS AND EXAMPLES

APPLYING THESE EXPANSION AND CONDENSATION TECHNIQUES ALLOWS FOR SOLVING MANY TYPES OF PROBLEMS EFFICIENTLY.

EXAMPLE 1: SIMPLIFY A COMPLEX LOGARITHMIC EXPRESSION

SIMPLIFY:

$$\left[\log_2 (8x^3) - 2 \log_2 x + \log_2 4 \right]$$

STEP-BY-STEP SOLUTION:

- EXPAND $\log_2 (8x^3)$:

$$\left[\log_2 8 + \log_2 x^3 = 3 + 3 \log_2 x \right]$$

- EXPAND $2 \log_2 x$:

$$\left[2 \log_2 x \right]$$

- EXPAND $\log_2 4$:

$$\left[\right]$$

2
\\

- REWRITE THE ENTIRE EXPRESSION:

$$\begin{aligned} & \\ & (3 + 3 \log_2 x) - 2 \log_2 x + 2 \\ & \end{aligned}$$

- COMBINE LIKE TERMS:

$$\begin{aligned} & \\ & 3 + (3 \log_2 x - 2 \log_2 x) + 2 = 3 + \log_2 x + 2 \\ & \end{aligned}$$

- FINAL SIMPLIFIED EXPRESSION:

$$\begin{aligned} & \\ & 5 + \log_2 x \\ & \end{aligned}$$

RESULT:

$$\begin{aligned} & \\ & \boxed{\log_2 (8x^3) - 2 \log_2 x + \log_2 4 = 5 + \log_2 x} \\ & \end{aligned}$$

EXAMPLE 2: CONDENSE A LOGARITHMIC EXPRESSION

GIVEN:

$$\begin{aligned} & \\ & \log_3 2 + 2 \log_3 5 - \log_3 8 \\ & \end{aligned}$$

SOLUTION:

- REWRITE THE TERMS:

$$\begin{aligned} & \\ & \log_3 2 + \log_3 5^2 - \log_3 8 \\ & \end{aligned}$$

$$\begin{aligned} & \\ & = \log_3 2 + \log_3 25 - \log_3 8 \\ & \end{aligned}$$

- COMBINE THE

Expanding And Condensing Logarithms

expanding and condensing logarithms: ACT Math in 30 Days Reza Nazari, 2021-05-03 A Fast, Innovative Way to Put You on the Path to Your Best Score Want to ace the ACT Math test in less than 30 days? This book could be exactly what you're looking for! Allow a top test prep expert to hold your hand and guide you step by step to ACT Math Success! The author knows exactly what students need to study and focus on so that they can rapidly improve their ACT Math test scores! This book features: □ Content that is 100% aligned with the 2021 ACT test □ A beginner-friendly

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expanding and condensing logarithms: *ACT Math for Beginners* Reza Nazari, 2020-07-10
ACT Mathematics test-takers' #1 Choice! Recommended by Test Prep Experts! A PERFECT Math Prep book to help you ACE the ACT Mathematics test! The perfect guide for students of every level, ACT Math for Beginners will help you incorporate the most effective methods and all the right strategies to get ready for your ACT Math test! This up-to-date guide reflects the 2023 test guidelines and will set you on the right track to hone your math skills, overcome exam anxiety, and boost your confidence. Are you ready to ace the ACT Math test? ACT Math for Beginners creates confident, knowledgeable students that have all the skills they need to succeed on the ACT. It builds a solid foundation of mathematical concepts through easy-to-understand lessons and basic study guides. Not only does this all-inclusive workbook offer everything you will ever need to conquer the ACT Math test, but it also contains two full-length and realistic ACT Math tests that reflect the format and question types on the ACT to help you check your exam-readiness and identify where you need more practice. With this book, students will learn math through structured lessons, complete with a study guide for each segment to help understand and retain concepts after the lesson is complete. It includes everything from: Content 100% aligned with the 2023 ACT test Written by ACT Math tutors and test experts Complete coverage of all ACT Math concepts and topics on the 2023 ACT test Step-by-step guide for all ACT Math topics Over 500 additional ACT math practice questions in both multiple-choice and grid-in formats with answers grouped by topic (so you can focus on your weak areas) Abundant Math skills building exercises to help test-takers approach unfamiliar question types 2 full-length practice tests (featuring new question types) with detailed answers And much more! With this self-study guide, you won't need a math tutor to pave your path to success. ACT Math for Beginners is the only book you'll ever need to master ACT Math concepts and ace the ACT Math test! Ideal for self-study and classroom usage! Visit www.EffortlessMath.com for Online Math Practice

expanding and condensing logarithms: *ALEKS Math for Beginners* Reza Nazari, 2020-07-10
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